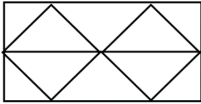


## REAL TEST

ECE

- Q1** In the figure shown below, various horizontal and vertical segments divide the outer shape into multiple regions. How many rectangles and triangles are there in the figure?



- (A) Two rectangles & Twelve triangles  
 (B) Five rectangles & Ten triangles  
 (C) Six rectangles & Twelve triangles  
 (D) Eight rectangles & Eleven triangles

- Q2** Train P leaves station A at 08:00 hours and reaches station B at 12:00 noon. Train Q leaves station B at 09:00 hours and reaches station A at 15:00 hours. Assuming both trains travel at constant speeds, at what exact time do the two trains cross each other?

- (A) 10:15 hours  
 (B) 10:36 hours  
 (C) 10:48 hours  
 (D) 11:30 hours

- Q3** Two fair dice are thrown simultaneously. In how many possible outcomes is the number shown on the top face of the first die greater than the number on the bottom face of the second die?

- (A) 18 (B) 36  
 (C) 6 (D) 15

- Q4** Select the most appropriate meaning of the underlined idiom.

The actor decided to live life **in the fast lane**.

- (A) Racing away to the moon  
 (B) A life of extreme speed  
 (C) A life filled with excitement  
 (D) Dropping charges of crime

- Q5** Select the most appropriate synonym of the given word.

**LUCID**

- (A) Lucky (B) Timely  
 (C) Clear (D) Happy

- Q6** Which of the following powers of 6 is the largest factor of :  $1 \times 2 \times 3 \times 4 \times 5 \dots \times 89 \times 90$ .

- (A)  $6^{24}$  (B)  $6^{44}$   
 (C)  $6^{34}$  (D)  $6^{18}$

- Q7** In a bakery, Rohan can bake half as many cakes as Meera in one-sixth of the time it takes Meera. If they decide to work together, they can bake all the cakes in 10 days. How many days would Meera need to bake all the cakes by herself?

- (A) 40 days (B) 25 days  
 (C) 30 days (D) 35 days

- Q8** The given sentence contains a grammatical error. Identify the segment that contains the error.

Smitha was offered the job although having no qualifications.

- (A) although having  
 (B) Smitha was offered  
 (C) the job  
 (D) no qualifications

- Q9** A rectangular sheet of cardboard has its sides in the ratio 1:4. Riya keeps cutting it in half along the longer side. After several cuts, she wonders: after how many cuts will the rectangle again have the same 1:4 ratio of sides?

- (A) 4 cuts (B) 6 cuts  
 (C) 3 cuts (D) Never

- Q10** A chef intends to fill a display case with 20 cupcakes, reaching its full capacity. Every 30 seconds, he adds 2 cupcakes, but a mischievous helper takes 1 cupcake out. How much time will it take for all 20 cupcakes to be in the display case for the first time?

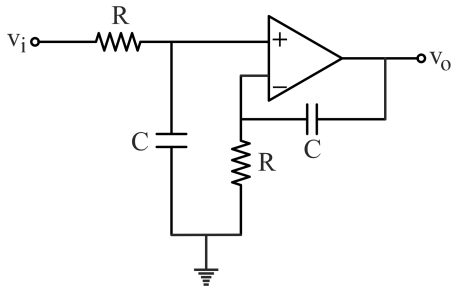
- (A) 600 seconds (B) 328 seconds  
 (C) 570 seconds (D) 300 seconds

- Q11** An isotropic antenna is radiating power 100 W. The strength of electric and magnetic field strength at a distance 5 m from the antenna, are \_\_\_\_\_ and \_\_\_\_\_ respectively.

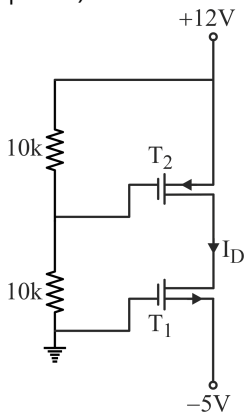
- (A) 21.9 V/m, 58.1 mA/m  
 (B) 15.5 V/m, 41.1 mA/m  
 (C) 10.95 V/m, 29.06 mA/m  
 (D) None



- Q12** If the op-amp shown in figure below is ideal, then the circuit acts as



- (A) Low pass filter  
(B) Bandpass filter  
(C) All pass filter  
(D) High pass filter
- Q13** To implement 3-input XOR operation using 2-input NAND gate, number of NAND gate required will be \_\_\_\_.
- Q14** In a p-type MOSFET, inversion channel is created at certain gate to source voltage. Inversion channel is dominated by  
(A) Electrons (B) Holes  
(C) Acceptor ions (D) Donor ions
- Q15** For the given MOSFET arrangement, threshold voltage  $|V_T| = 2V$  and  $k_n' \left(\frac{W}{L}\right) = 0.1 \text{ mA/V}^2$ . The maximum value of drain current is \_\_\_\_mA. (Rounded off to two decimal places)



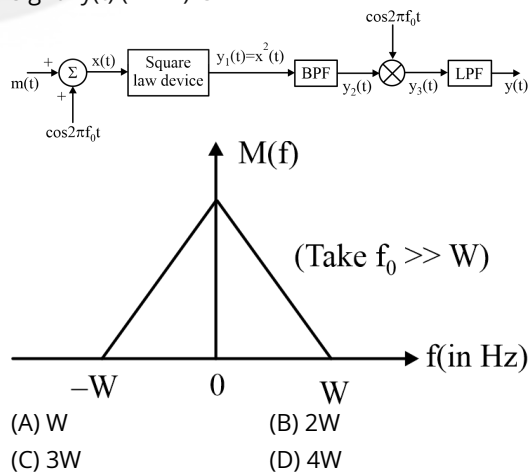
- Q16** For  $x(n) = \cos\left(\frac{\pi n}{2}\right)$ , the DTFS coefficients are represented as  $c_k$ , then choose the correct option(s):  
(A)  $C_1$  is non zero (B)  $C_1$  is zero  
(C)  $C_3$  is non zero (D)  $C_7$  is non zero

- Q17** In a pure - SC, trivalent impurity is added with concentration  $N_A = \frac{3 n_i}{2}$ , where  $n_i$  is intrinsic carrier conc<sup>n</sup> then?  
(A) It is n-type SC with  $n = \frac{3 n_i}{2}$   
(B) It is p-type SC with  $p = \frac{3 n_i}{2}$   
(C) It is p-type SC with  $p = 2n_i$   
(D) It is p-type SC with  $n = \frac{2}{3} n_i$

- Q18** A survey was conducted among 800 College students. The results for their preference for three subjects: Mathematics(M), Physics(P) and Chemistry(C) are as follows:

- 350 students like M, 300 students like P, 250 students like C.
  - 150 students like both M and P, 100 students like both P and C.
  - 120 students like both M and C.
  - 70 students like all three subjects (M, P and C)
- How many students do not like any of the three subjects?  
(A) 600 (B) 370  
(C) 450 (D) 200

- Q19** A message signal  $m(t)$  whose spectrum  $M(f)$  is passed through a system as shown below. The BPF (Band Pass Filter) has a bandwidth of  $2W$  Hz centered at  $f_0$  and the LPF (Low pass filter) has a bandwidth of  $W$ Hz. The bandwidth of the signal  $y(t)$  (in Hz) is



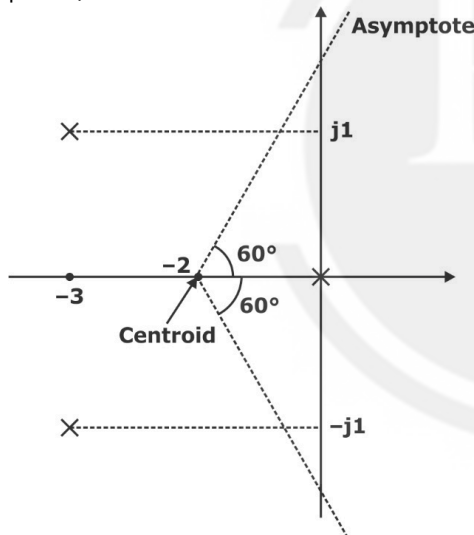
**Q20** It is desired to construct uniform transmission lines using polyethylene ( $\epsilon_r = 2.25$ ) as the dielectric medium. The distance of separation for  $300 \Omega$  two-wire transmission line, where radius of the conducting wires is 0.6 mm, is \_\_\_\_\_ (mm).

- (A) 25.51 (B) 7.31  
(C) 14.62 (D) 12.76

**Q21** A Boolean function is given as:  $f(A, B, C) = \overline{A}B + \overline{A}C + BC$  it will further simplify to

- (A)  $\overline{A}B + \overline{A}C$   
(B)  $\overline{A}B + BC$   
(C)  $\overline{A}C + BC$   
(D) No simplification is possible

**Q22** The figure shown the asymptote root locus in real axis and location of poles and centred, then the ratio  $\left(\frac{\text{break in}}{\text{break away}}\right)$  point of the root locus is \_\_\_\_\_. (Rounded off to two decimal places).



**Q23** If  $X(t)$  and  $Y(t)$  are two orthogonal stationary random processes and two other processes  $U(t)$  and  $V(t)$  are formed as follows:

$$U(t) = X(t) + Y(t)$$

$$V(t) = 2X(t) + 3Y(t)$$

The which of the following is true ?

- (A)  $R_U(\tau) = R_X(\tau) - R_Y(\tau)$   
(B)  $R_V(\tau) = R_X(\tau) + 3R_Y(\tau)$   
(C)  $R_{UV}(\tau) = 4R_X(\tau) + 9R_Y(\tau)$   
(D)  $R_{UV}(\tau) = 2R_X(\tau) + 3R_Y(\tau)$

**Q24** A logic circuit implements the Boolean function  $F = \overline{x}y + x\overline{y}z + xy\overline{z}$ . It is found that the input combination  $x = z = 1$  can never occur. Taking this into account, a simplified expression for  $F$  is given by

- (A)  $x + z$  (B)  $y + z$   
(C)  $x + y$  (D)  $x + y + z$

**Q25** Let  $m_1(t)$  and  $m_2(t)$ , be two message signal and let  $y_1(t)$  and  $y_2(t)$  be the corresponding modulated version.

Which of the following statement is/are correct?

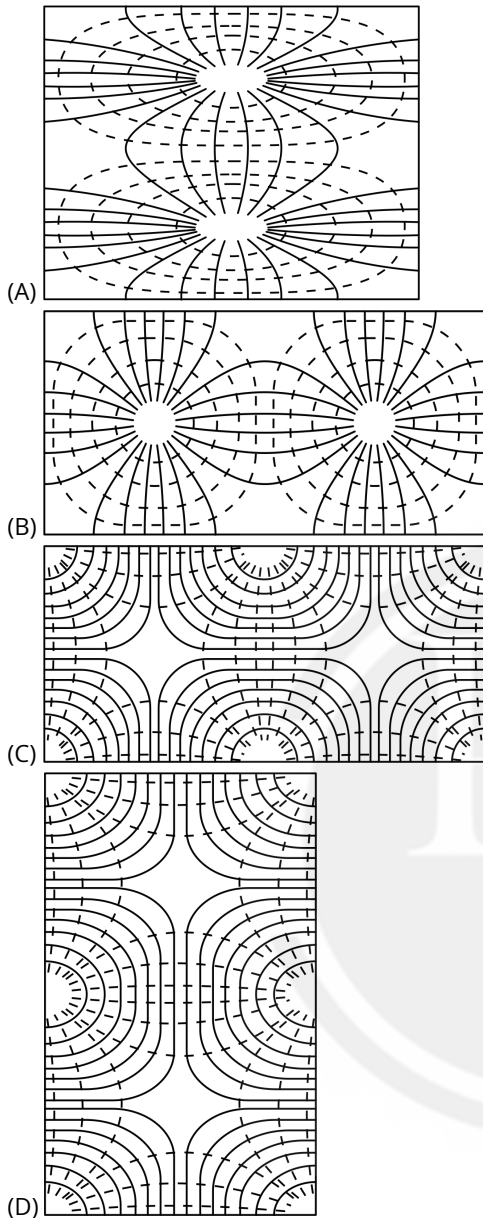
- (A) When the combined message signal  $m_1(t)$  and  $m_2(t)$  DSB modulate a carrier  $A_c \cos 2\pi f_c t$ , the result is the sum of the DSB amplitude-modulated signals  $y_1(t)$  and  $y_2(t)$ .  
(B) If  $m_1(t)$  and  $m_2(t)$  frequency modulates a Carrier, the modulated signal is equal to the sum of  $y_1(t)$  and  $y_2(t)$   
(C) When the combined message signal  $m_1(t)$  and  $m_2(t)$  DSB modulate a carrier  $A_c \cos 2\pi f_c t$ , the result is not equal to the sum of the DSB amplitude-modulated signals  $y_1(t)$  and  $y_2(t)$ .  
(D) If  $m_1(t)$  and  $m_2(t)$  frequency modulates a Carrier, the modulated signal is not equal to the sum of  $y_1(t)$  and  $y_2(t)$

**Q26** An air filled rectangular waveguide with dimensions 'a' and 'b' that will operates in the dominant  $TE_{10}$  mode at  $f = 10$  GHz. The minimum value of 'a' of the waveguide which should be chosen so that at  $f = 10$  GHz the waveguide not only operated on the single  $TE_{10}$  mode but also that  $f = 10$  GHz is simultaneously 25% above the cut-off frequency of the dominant  $TE_{10}$  mode, is \_\_\_\_\_ cm.

- (A) 0.9375 (B) 1.875  
(C) 3.75 (D) 1.2



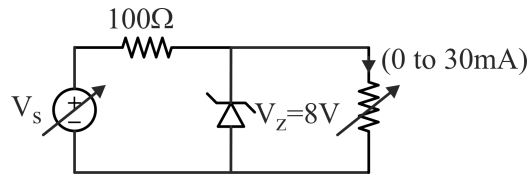
**Q27** Which of the following will represent field pattern of  $TM_{21}$  in rectangular wave guide ?



**Q28**  $L = \lim_{x \rightarrow 0} \left(\frac{1}{x}\right)^{\tan x}$

- (A)  $L = 0$
- (B)  $L = \frac{1}{e}$
- (C)  $L = e$
- (D)  $L = 1$

**Q29** An 8 V Zener diode voltage regulator as shown in figure below operates from a source that varies from 12 V to 18 V. The series resistance is  $100 \Omega$  and the load draws current that varies from 0 mA to 30 mA. Then which of the following is/are correct under worst-case conditions?



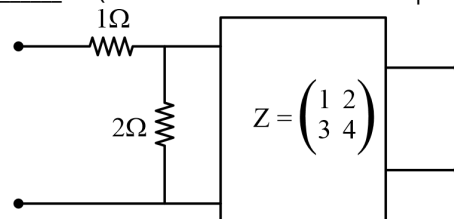
- (A)  $P_{Z(max)} = 80 \text{ mW}$
- (B)  $P_{Z(max)} = 800 \text{ mW}$
- (C)  $I_{Z(max)} = 10 \text{ mA}$
- (D)  $I_{Z(max)} = 100 \text{ mA}$

**Q30** Q. Which of the following statements is/are correct?

- (A) A demultiplexer cannot be used as a decoder.
- (B) A demultiplexer selects one of many outputs.
- (C) The input to output pin ratio of a multiplexer with n control inputs is  $2^n : 1$ .
- (D) The dual of an expression  $(\overline{A}B + BC + \overline{C}D)$  is  $(\overline{A} + B)(B + C)(\overline{C} + D)$ .

**Q31** For  $\log(1 - 5z)$  with  $|z| < \frac{1}{5}$ , the Inverse Z-transform is given by  $\frac{\alpha^n u(-\beta n - 1)}{n}$ ; then the value of  $\alpha\beta$  is \_\_\_\_\_. (Rounded off to two decimal places)

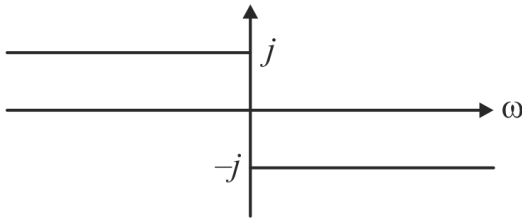
**Q32** Consider below given circuit, then the value of  $Z_{12}$  of the complete 2-port network will be \_\_\_\_\_  $\Omega$ . (Rounded off to two decimal places)



**Q33** Reverse saturation current of a pn junction diode is  $I_0 = 10^{-8} \text{ A}$ . Diode is at equilibrium at no applied bias, then the value of diffusion current flowing through diode (from p to n direction) \_\_\_\_\_ nA.



**Q34** Fourier transform of signal  $h(t)$  is  $H(\omega)$ .  $H(\omega)$  is shown in the figure below. Then  $h(t)$  is



- (A)  $\frac{2}{\pi t}$                       (B)  $\frac{1}{\pi t}$   
 (C)  $\frac{j}{\pi t}$                         (D)  $\frac{-j}{\pi t}$

**Q35** Let  $X$  and  $Y$  be two independent random variables.  $\text{Var}(X) = 4$  and  $\text{Var}(Y) = 9$ . Choose the correct option(s) given below.

- (A)  $\text{Var}(2X) = 8$   
 (B)  $\text{Var}(X - Y) = 13$   
 (C)  $\text{Var}(2X - 3Y) = 97$   
 (D)  $\text{Var}(Y/3) = 1$

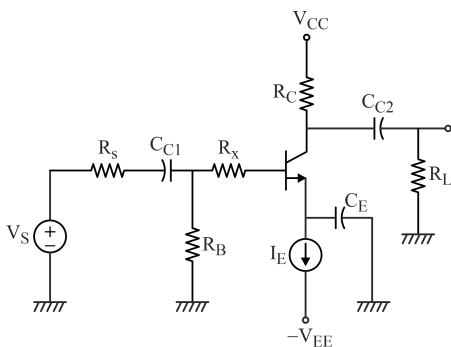
**Q36** The value of the following series  $\frac{1}{2} - \frac{1}{6} + \frac{1}{24} - \frac{1}{120} + \dots$  is \_\_\_\_ (Round off to two decimal places).

**Q37** Consider the system of linear equations  
 $x + y + 5z = 3$   
 $x + 2y + 2z = 5$   
 $2x + 4y + 4z = k$

For the system to have infinitely many solutions, the value of  $k$  is \_\_\_\_ (Enter in integer)

**Q38** For a CE amplifier shown below upper 3-dB cut-off frequency is \_\_\_\_ kHz, provided below:

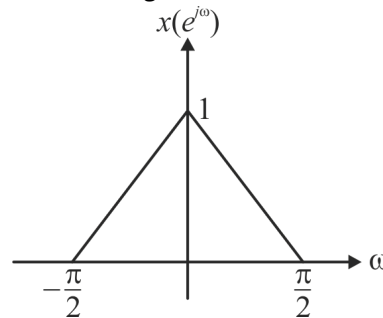
- (i) Unity gain frequency = 800 MHz  
 (ii)  $C_{\mu} = 1$  pF  
 (iii)  $C_{\pi} = 7$  pF  
 (iv)  $r_{\pi} = 2.5$  k $\Omega$   
 (v)  $r_0 = 100$  k $\Omega$   
 (vi)  $V_{CC} = 10$  V =  $-V_{EE}$   
 (vii)  $R_S = R_L = 5$  k $\Omega$   
 (viii)  $R_C = 8$  k $\Omega$ ,  $R_x = 50$   $\Omega$ ,  $R_B = 100$  k $\Omega$   
 (ix)  $\beta = 100$ ,  $I_E = 1$  mA



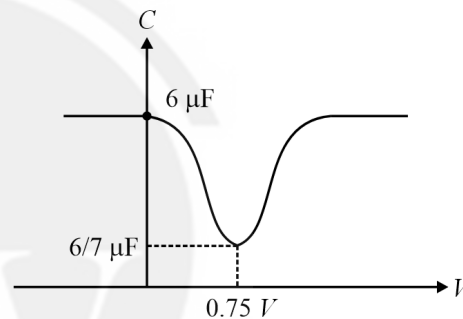
- (A) 560                              (B) 630  
 (C) 762                              (D) 875

**Q39** For a signal  $x(n)$ , its DTFT is shown below such

that a constant  $A$  is given by  $\frac{\sum_{n=-\infty}^{\infty} nX(n)}{\sum_{n=-\infty}^{\infty} X(n)}$ . Then the value of  $A$  is \_\_\_\_\_. (Rounded off to nearest integer)

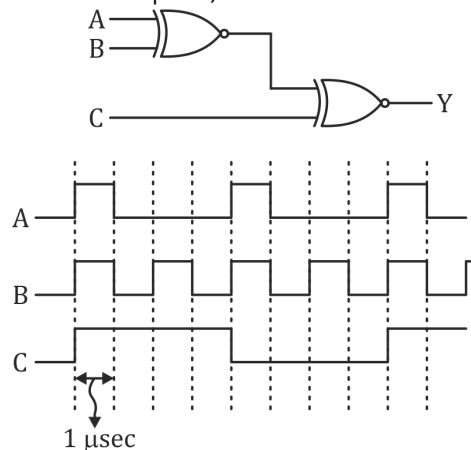


**Q40** C-V characteristic of a MOS capacitor is given below:

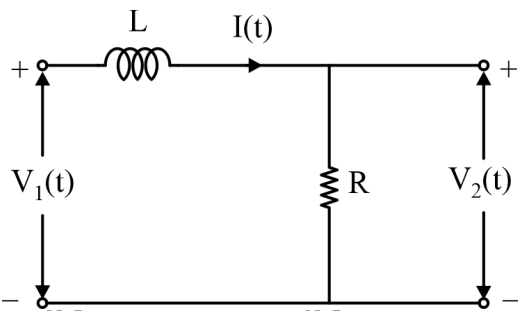


If area of cross section  $A = 1$  cm<sup>2</sup> and substrate doping is  $N_s = 2 \times 10^{16}$ /cm<sup>3</sup> then value of maximum electric field inside substrates in depletion mode of operation is \_\_\_\_ kV/cm.

**Q41** The waveform of three periodic signals A, B and C are shown in the figure below. If they are applied to the two EX-NOR gate combination circuits, then the frequency of output 'Y' will be \_\_\_\_ kHz. (Rounded off to one decimal place)

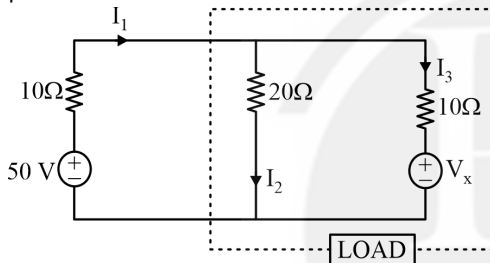


**Q42** Consider the circuit shown below. If the two sided power spectral density of  $V_1(t)$  is given as,  $S_{V_1}(f) = \frac{N_0}{2} W/Hz$ . Then the average power of  $V_2(t)$  will be



- (A)  $\frac{N_0 R}{4L} Watts$       (B)  $\frac{N_0 R}{2L} Watts$   
 (C)  $\frac{N_0 4L}{R} Watts$       (D)  $\frac{2N_0 L}{R} Watts$

**Q43** For the circuit shown below, which of the following is/are correct so that maximum power is transferred to load?



- (A)  $V_x = 10V$       (B)  $I_1 = 2.5 A$   
 (C)  $I_2 = 1.25 A$       (D)  $I_3 = 1A$

**Q44** For a system,  $CLTF = \frac{10(s+3)}{s^3+6s^2+11s+6}$ . If the state space representation of the system is  $\dot{x}(t) = \dots$

$$\dot{x}(t) = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix} x(t) + \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix} u(t)$$

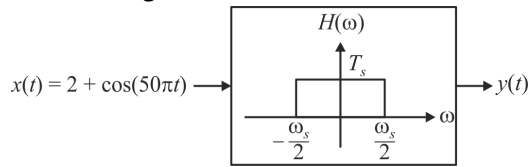
,  $y(t) = [C_1 C_2 C_3] x(t)$ .  
 then  $\frac{b_1+C_1}{b_2+C_2}$  is \_\_\_\_\_. (Rounded off to one decimal place).

- (A) 2      (B) 3  
 (C) 4      (D) 5

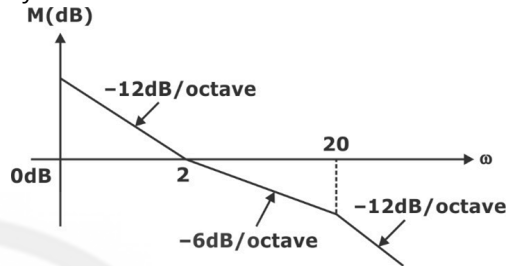
**Q45** If the Fourier transform of  $x_1(t) = te^{-|t|}$  is  $X_1(\omega)$  and of  $x_2(t) = \frac{4}{(1+t^2)^2}$  is  $X_2(\omega)$  then  $\frac{X_1(\omega)}{X_2(\omega)}$  at  $\omega = \pi$  rad/sec is \_\_\_\_\_. (Rounded off to two decimal places).

**Q46** The inverse Laplace transform is given as  $L^{-1} \left\{ \frac{s+3}{s^2-4s+13} \right\} = e^{2t} \{ \cos 3t + \alpha \cdot \sin 3t \}$   
 The value of 'α' is \_\_\_\_\_. (Round off to three decimal places)

**Q47** A signal  $x(t)$  is sampled at 0.01 sec, such that its output  $y(t)$  is  $A + \cos(\omega t)$  as shown below. The value of A is \_\_\_\_\_. (Rounded off to nearest integer)

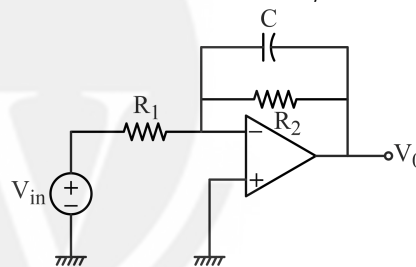


**Q48** The magnitude plot for a minimum phase system is shown



The steady state error for  $\frac{5t^2}{2}$  input is \_\_\_\_\_. (Rounded off to two decimal places).

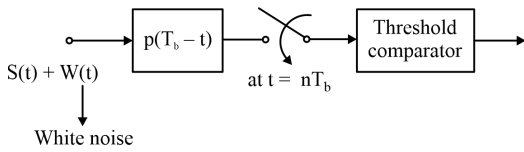
**Q49** For the circuit shown below, if



- (A)  $\omega \gg \frac{1}{R_2 C}$ , circuit will behave like integrator  
 (B)  $\omega \ll \frac{1}{R_2 C}$ , circuit will behave like amplifier  
 (C)  $\omega \gg \frac{1}{R_2 C}$ , circuit will behave like amplifier  
 (D)  $\omega \ll \frac{1}{R_2 C}$ , circuit will behave like integrator



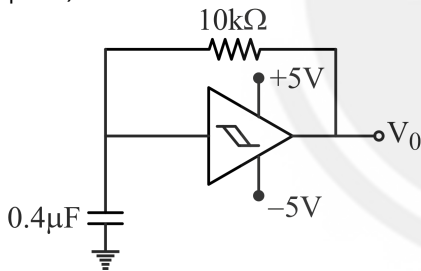
**Q50** Binary data is transmitted through an AWGN channel with power spectral density of  $h/2$  W/Hz using a pulse  $p(t)$  for logic-0 and a pulse  $3p(t)$  for logic-1. The signal is received by using a matched filter receiver as shown below



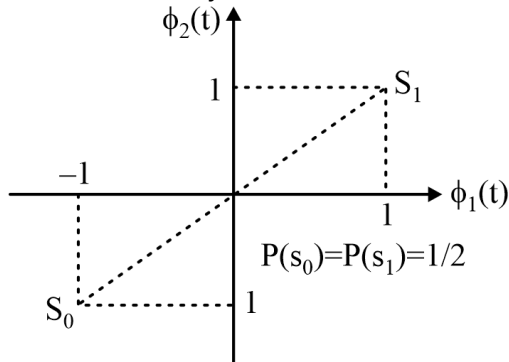
The duration of the pulse  $p(t)$  is  $T_b$  and the energy associated with the pulse  $p(t)$  is  $E_p$ . If logic-0 and logic-1 are equiprobable and optimum threshold used by the threshold comparator, then the bit error rate (BER) will be [Q(x) indicates Q-function and  $E_b$  is the average bit energy]

- (A)  $Q\left(\sqrt{\frac{2E_b}{\eta}}\right)$
- (B)  $Q\left(\sqrt{\frac{E_b}{\eta}}\right)$
- (C)  $Q\left(\sqrt{\frac{0.8E_b}{\eta}}\right)$
- (D)  $Q\left(\sqrt{\frac{0.4E_b}{\eta}}\right)$

**Q51** A hysteresis type TTL inverter is used to realize an oscillator in the circuit.  $V_{LT} = 0.9V$ ,  $V_{UT} = 1.8V$ , the period for which output is 'high is \_\_\_\_\_ msec. (Rounded off to three decimal place).



**Q52** The constellation diagram of a binary modulation scheme is shown below. The two equiprobable symbols shown in the diagram are transmitted through an AWGN channel with noise  $PSD = \frac{1}{2} W/Hz$ . If a correlator receiver with optimum threshold detection is used at the receiver end, then the Bit Error Rate (BER) of the system will be



- (A) Q(1)
- (B) Q(2)
- (C) Q(3)
- (D) Q(4)

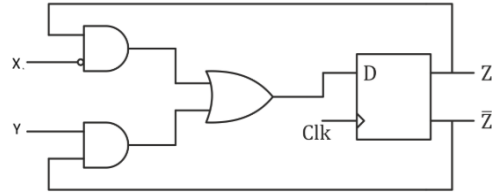
**Q53** Consider the following D.E:

$$y'' + y = \sin(t)$$

with initial conditions as  $y(0) = 0$  and  $y'(0) = 0$ .

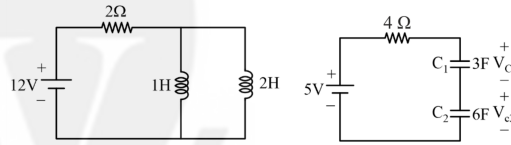
The value of  $y(\pi)$  is \_\_\_\_\_ (Round off to two decimal places)

**Q54** A sequential circuit using D flip-flops and logic gates is shown below. When X and Y are the inputs and Z is the output. Then the circuit is

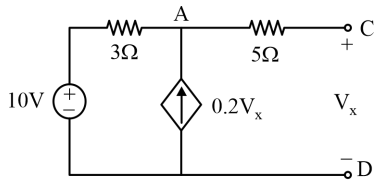


- (A) S-R FF with inputs  $X = R$  and  $Y = S$
- (B) S-R FF with inputs  $X = S$  and  $Y = R$
- (C) J-K FF with inputs  $X = J$  and  $Y = K$
- (D) J-K FF with inputs  $X = K$  and  $Y = J$

**Q55** If the steady state voltage across the capacitor 6 F is  $V_{C2}(\infty)$  and current in the inductor 1H is  $i_1(\infty)$ , then  $\frac{V_{C2}(\infty)}{i_1(\infty)}$  is \_\_\_\_\_ mΩ. (Rounded off to two decimal places).

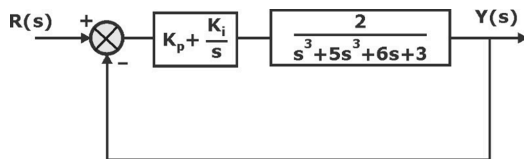


- Q56** The circuit shown in figure, contains a dependent current source between A and B terminals. The Thevenin's equivalent circuit across terminals C and D.



- (A)
- (B)
- (C)
- (D)

- Q57** A unity feedback control system that uses proportional integral controller is shown in figure below. The stability of closed loop system is controlled by proportional integral controller. The maximum value of  $K_i$  and corresponding value of  $K_p$  for the system to be stable are



- (A)  $K_i = 4.5$  (B)  $K_p = 6$   
 (C)  $K_p = 13.5$  (D)  $K_i = 5$

- Q58** If  $a, b$  and  $c$  are the roots of  $x^3 - 5x + 3 = 0$ , then the value of the determinant  $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$  is equal to \_\_\_\_\_.

- Q59** Which of the following is NOT correct?  
 (A) Indirect bandgap SCs are not used for designing of LED.  
 (B) MOSFET is used as voltage variable resistance in triode region at low  $V_{DS}$ .  
 (C) Due to early effect, current gain of BJT decreases  
 (D) In reverse bias diode maximum electric field is at junction

- Q60** Which of the following statement(s) is/are correct regarding a vector field  $\vec{A}$ .

- (A)  $\vec{\nabla} \cdot \vec{A} = 0$ ,  $\vec{A}$  is solenoidal  
 (B)  $\vec{\nabla}^2 \vec{A} = 0$ ,  $\vec{A}$  is solenoidal  
 (C)  $\vec{\nabla} \times (\vec{\nabla} \times \vec{A}) = \vec{\nabla} (\vec{\nabla} \cdot \vec{A}) - \nabla^2 \vec{A}$   
 (D)  $\vec{\nabla} \cdot (\vec{\nabla} \times \vec{A}) = 0$

- Q61** In a n-type MOSFET operating in depletion mode, following information is given:

Surface potential  $\phi_s = 0.45$  V

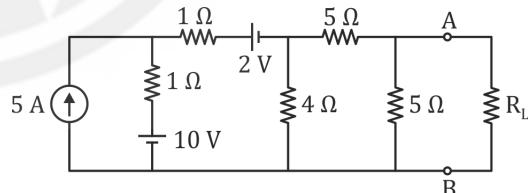
Depletion region width inside substrate  $W = 10\mu\text{m}$

Maximum electric field inside oxide layer will be

Given:  $\frac{\epsilon_{Si}}{\epsilon_{SiO_2}} = 2.5$

- (A) 0.9 kV/cm (B) 2.25 kV/cm  
 (C) 0.36 kV/cm (D) None of these

- Q62** Consider the network shown below,



The value of norton's current and norton's resistance are

- (A)  $I_N = 2.53\text{A}, R_N = 1.87\Omega$   
 (B)  $I_N = 1.37\text{A}, R_N = 2.79\Omega$   
 (C)  $I_N = 2.53\text{A}, R_N = 2.79\Omega$   
 (D)  $I_N = 1.37\text{A}, R_N = 1.87\Omega$

- Q63** A  $50\Omega$  lossless transmission line is terminated in a load impedance  $Z_L = R_L + jX_L$ . The relation between ' $R_L$ ' and ' $X_L$ ' in order that the standing wave ratio on the line is 2, is a circle of radius ' $R$ '. The value of ' $R$ ' is \_\_\_\_\_( $\Omega$ )



**Q64** For a (7, 4) linear block code, the parity check matrix is given by

$$\bar{H} = \left[ \begin{array}{ccc|ccc} 1 & 0 & 0 & 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 & b & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & a \end{array} \right]$$

If it is known that "0100011" is a valid codeword for the given code, then the value of 'a' and 'b' are respectively.

- (A) 0 and 0                      (B) 0 and 1  
(C) 1 and 0                      (D) 1 and 1

**Q65** If the current density given by  $\vec{J} = r\hat{a}_r - \sin\theta\hat{a}_\theta + 3\hat{a}_\phi$  A/m<sup>2</sup>, the magnitude of the current crossing the surface defined by  $r = 2\text{m}$ ,  $0 \leq \theta \leq 90^\circ$ ,  $30^\circ \leq \phi \leq 60^\circ$  is \_\_\_\_.



# Answer Key

|     |           |     |           |
|-----|-----------|-----|-----------|
| Q1  | B         | Q34 | B         |
| Q2  | C         | Q35 | B, C, D   |
| Q3  | D         | Q36 | 0.35~0.38 |
| Q4  | C         | Q37 | 10~10     |
| Q5  | C         | Q38 | C         |
| Q6  | B         | Q39 | 0~0       |
| Q7  | A         | Q40 | 3.2~3.2   |
| Q8  | A         | Q41 | 125~125   |
| Q9  | D         | Q42 | A         |
| Q10 | C         | Q43 | B, C      |
| Q11 | C         | Q44 | B         |
| Q12 | A         | Q45 | 0.45~0.55 |
| Q13 | 8~8       | Q46 | 1.6~1.67  |
| Q14 | B         | Q47 | 2~2       |
| Q15 | 0.44~0.46 | Q48 | 1.2~1.3   |
| Q16 | A, C      | Q49 | A, B      |
| Q17 | C         | Q50 | D         |
| Q18 | D         | Q51 | 0.98~1    |
| Q19 | A         | Q52 | B         |
| Q20 | A         | Q53 | 1.5~1.6   |
| Q21 | D         | Q54 | D         |
| Q22 | 2.35~2.4  | Q55 | 410~420   |
| Q23 | D         | Q56 | B         |
| Q24 | C         | Q57 | A, B      |
| Q25 | A, D      | Q58 | 0~0       |
| Q26 | B         | Q59 | C         |
| Q27 | B         | Q60 | A, C, D   |
| Q28 | D         | Q61 | B         |
| Q29 | B, D      | Q62 | B         |
| Q30 | B, C, D   | Q63 | 37.3~37.8 |
| Q31 | 0.2~0.2   | Q64 | D         |
| Q32 | 1.31~1.35 | Q65 | 1~1.1     |
| Q33 | 10~10     |     |           |

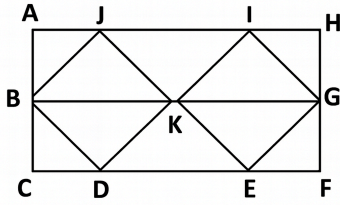


# Hints & Solutions

Note: scan the QR code to watch video solution

## Q1 Text Solution:

Pointing the figure as



The Rectangles are :

ABGH, BCFG, ACFH, BDKJ & KEGI. Total 5.

The Triangles are:

ABJ, BJK, JKI, IKG, IHG, BCD, BDK, KDE, KEG & GEF. Total 10.

## Q2 Text Solution:

If the distance between Stations A and B is D km

Train P speed =  $D/4$  (covers in 4 hours i.e. 0800 to 1200)

Train Q speed =  $D/6$  (covers in 6 hours i.e. 0900 to 1500)

To reach the meeting point, Distance covered by Train P + Distance covered by Train Q = Total Distance (D).

Let's say they meet after 'x' hours from 0800.

Thus,  $x(D/4) + (x-1)(D/6) = D$

Or  $(x/4) + (x-1)/6 = 1$

Or  $3x + 2x - 2 = 12$

Or  $5x = 14$

Thus  $x = 14/5 = 2$  and  $4/5$  hours = 2 hours 48 minutes

From 0800, 2 hours 48 minutes = 10:48 hours

## Q3 Text Solution:

If top face of 1<sup>st</sup> die is 2, then second die is 1 (Only 1 case)

If top face of 1<sup>st</sup> die is 3, then second die is 1 or 2 (2 cases)

If top face of 1<sup>st</sup> die is 4, then second die is 1 or 2 or 3 (3 cases)

Similarly, If top face of 1<sup>st</sup> die is 5, then 4 cases

If top face of 1<sup>st</sup> die is 6, then 5 cases.

Total  $1 + 2 + 3 + 4 + 5 = 15$

## Q4 Text Solution:

The idiom "live life in the fast lane" means a life filled with excitement Option C.

## Q5 Text Solution:

Lucid means easy to understand, clear, transparent in meaning or thought.

## Q6 Text Solution:

As 6 is formed by the product of 3 and 2. Also number of 3's is less as compared to 2's. So, as many 3's those many 6's are formed.

To find in 90!

$\frac{90}{3}$  gives 30

$\frac{30}{3}$  gives 10

$\frac{10}{3}$  gives 3 (whole number)

$\frac{3}{3}$  gives 1

And  $\frac{1}{3}$  gives 0 (whole number).

Thus total  $30 + 10 + 3 + 1 = 44$ . Thus 90! has largest factor  $6^{44}$ .

## Q7 Text Solution:

If Meera bakes 1 cake in 1 unit time, Rohan bakes  $\frac{1}{6}$  cake in  $\frac{1}{6}$  unit time.

Or Rohan bakes 1 cake  $\frac{2}{6}$  unit time.

Comparing Time taken to do the work

Meera : Rohan =  $1 : \frac{1}{3} = 3 : 1$

If Rohan takes x days, Meera takes 3x days.

Given that they do together the work in 10 days, i.e.  $(\frac{1}{x}) + (\frac{1}{3x}) = \frac{1}{10}$

Or  $(\frac{4}{3x}) = \frac{1}{10}$  Or  $\frac{3x}{4} = 10$  Or  $x = \frac{40}{3}$ .

Thus Meera takes  $3(\frac{40}{3}) = 40$  days.

## Q8 Text Solution:

"Although" is a conjunction and must be followed by a subject + finite verb (e.g., "although she had no qualifications").

Here it is incorrectly followed by just the participle "having", so the phrase is ungrammatical.

Correct versions would be:

- "Smitha was offered the job although she had no qualifications."
- "Smitha was offered the job despite having no qualifications."

## Q9 Text Solution:

Initial ratio 1 : 4.

Always cutting the longer side.

1<sup>st</sup> Cut ratio 1 : 2

2<sup>nd</sup> Cut ratio 1 : 1

3<sup>rd</sup> cut ratio (any side) 2 : 1.

4<sup>th</sup> Cut ratio again 1 : 1.

Thus Never it will come again to same ratio 1 : 4.



**Q10 Text Solution:**

In 30 seconds net cupcakes in display = 1 (2-1)

1 cup cake in 30 seconds

18 cupcakes in  $30 \times 18 = 540$  seconds.

In the next 30 seconds chef adds 2 cupcakes to make it 20.

Thus total earliest time =  $540 + 30 = 570$  seconds.

Note: The last moment can't be withdrawal as the display holds only 20 cupcakes.

**Q11 Text Solution:**

$$D_t = 1 \quad (\text{Directivity})$$

$$E_0 = \frac{\sqrt{30W_t D_t}}{R} = \frac{\sqrt{30 \times 100 \times 1}}{5} = 10.95 \text{ V/m}$$

$$H_0 = \frac{E_0}{\eta} = \frac{10.95}{120\pi} \text{ A/m} = 29.06 \text{ mA/m}$$

**Q12 Text Solution:**

$$V^+ = \frac{V_i}{(R + \frac{1}{Cs})} \cdot \frac{1}{Cs} = \frac{V_i}{sRC + 1} \quad \dots(i)$$

$$V_0 = \frac{V^+}{R} \cdot \frac{1}{Cs} + V^+ = V^+ \left(1 + \frac{1}{sRC}\right)$$

$$V_0 = V^+ \left(\frac{sRC + 1}{sRC}\right) \quad \dots(ii)$$

$$\frac{V_0}{V_i} = \frac{1}{sRC}$$

It is low pass filter.

Hence, option A is correct.

**Q13 Text Solution:**

3-input XOR operation is

$$y = A \oplus B \oplus C$$

For  $A \oplus B = P$  4 NAND gate - 2input

then  $y = P \oplus C$  4 NAND gate - 2input

So total 8 NAND gates of 2-input will be required.

**Q14 Text Solution:**

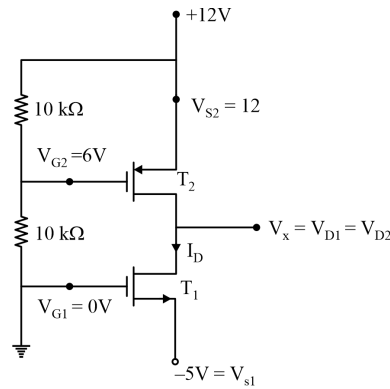
In p-type MOSFET Substrate is n-type and in n-type SC a inversion layer (channel) is created at certain gate to source voltage and majority charge carriers in inversion layer all holes.

**Q15 Text Solution:**

Given for both MOSFETS,  $|V_T| = 2V$

$$k'_n \left(\frac{W}{L}\right) = 0.1 \text{ mA/V}^2$$

Checking the values of saturation currents of both MOSFETs to find the maximum value of  $I_D$  :-



For  $T_1$  (NMOS):-

$$V_{G1} = 0V \quad V_{S1} = -5V \quad V_{D1} = V_x \text{ (Let)}$$

$$(V_{GS})_{T1} = V_{G1} - V_{S1} = 5V$$

$$\text{Overdrive voltage } (V_{GS} - V_T)_{T1} = 5 - 2 = 3V$$

$$(I_{D1})_{sat} = \frac{1}{2} k'_n \left(\frac{W}{L}\right) (V_{GS} - V_T)_{T1}^2$$

$$= \frac{1}{2} \times 0.1 \times 10^{-3} \times 9 = 0.45 \text{ mA}$$

Condition for saturation

$$(V_{DS})_{T1} > (V_{GS} - V_T)_{T1}$$

$$\Rightarrow V_x - (-5) > 3 \Rightarrow \boxed{V_x > -2V}$$

For  $T_2$  (PMOS):-

$$V_S = 12V, V_G = 6V, V_D = V_x, |V_T| = 2V$$

$$(V_{SG})_{T2} = V_S - V_G = 6V$$

Overdrive voltage

$$(V_{SG} - |V_T|)_{T2} = 6 - 2 = 4V$$

$$(I_{D2})_{sat} = \frac{1}{2} k'_p \left(\frac{W}{L}\right) (V_{SG} - |V_T|)_{T2}^2$$

$$= \frac{1}{2} \times 0.1 \times 10^{-3} \times 16 = 0.8 \text{ mA}$$

$$(I_{D1})_{sat} = 0.45 \text{ mA} \quad (I_{D2})_{sat} = 0.8 \text{ mA}$$

So, PMOS is capable of supplying more current.

Condition for saturation of  $T_2$  :-

$$V_S > (V_{SG} - |V_T|)$$

$$\Rightarrow 12 - V_x > 4 \Rightarrow \boxed{V_x < 8V}$$

As both the devices are connected in series and saturation currents for both are not equal, so they can't be in saturation simultaneously. NMOS saturation current 0.45 mA is much smaller than the saturation current of PMOS, so NMOS forces the current to reduce and hence PMOS must reduce its effective source to drain voltage  $V_{SD}$  so that it enters into its triode region.

As source is fixed at  $V_S = 12V$ , Voltage at drain of  $T_2$ , i.e.,  $V_x$  will have to increase to reduce  $V_{SD} (= V_S - V_D)$ .

Triode current equation of PMOS,

$$I_{D2} = \frac{1}{2} k'_p \left(\frac{W}{L}\right) [2(V_{SG} - |V_T|)V_{SD} - V_{SD}^2]$$

$$= \frac{1}{2} \times 0.1 \times 10^{-3} [2 \times 4 \times (12 - V_x) - (12 - V_x)^2]$$

$$= 0.05 \times 10^{-3} (12 - V_x) [8 - 12 + V_x]$$

$$I_{D2} \Rightarrow 0.05 \times 10^{-3} (12 - V_x) (V_x - 4)$$



Equating drain currents of  $T_1$  &  $T_2$  as they are in series

$$0.45 \times 10^{-3} = 0.05 \times 10^{-3} (12V_x - 48 - V_x^2 + 4V_x)$$

$$\Rightarrow 9 = -V_x^2 + 16V_x - 48$$

$$\Rightarrow V_x^2 - 16V_x + 57 = 0$$

$$\Rightarrow V_x = 10.645 \text{ or } V_x = 5.354$$

$$\text{For } V_x = 10.645 = V_{D1} = V_{D2},$$

$$\text{PMOS } T_2 \text{ Triode } I_{D2} = 0.45 \text{ mA}$$

$$\text{NMOS } T_1 \text{ saturation } I_{D1} = 0.45 \text{ mA}$$

So all conditions are satisfied hence we can say that NMOS works in saturation and limits the value of current to 0.45 mA and PMOS follows this current being in triode region.

So the maximum possible value of drain current  $I_D$  is 0.45 mA

#### Q16 Text Solution:

$$x(n) = \cos\left(\frac{\pi n}{2}\right)$$

$$\text{So, } \omega_0 = \frac{\pi}{2}$$

$$\text{Period} = \frac{2\pi}{\frac{\pi}{2}} = 4 \text{ i.e., } N_0 = 4$$

$$\text{So, } x(n) = \frac{1}{2} e^{j\omega_0 n} + \frac{1}{2} e^{-j\omega_0 n}$$

$$x(n) = \frac{1}{2} e^{j\frac{\pi}{2}n} + \frac{1}{2} e^{-j\frac{\pi}{2}n}$$

$$\text{DTFS } x(n) = \sum_{n=1}^{N_0-1} c_k e^{jk\omega_0 n} \quad \dots(1)$$

So, DTFS indices are:

$$k = 0, 1, 2, 3$$

Compare with,

$$e^{j\frac{\pi}{2}n} \Rightarrow k = 1$$

$$e^{-j\frac{\pi}{2}n} \Rightarrow e^{j(2\pi - \frac{\pi}{2})n} = e^{j\frac{3\pi}{2}n} \Rightarrow k = 3$$

This gives  $C_1 = \frac{1}{2}$  and  $C_3 = \frac{1}{2}$ , both are non-zero quantities.

#### Q17 Text Solution:

$$\text{Trivalent impurity conc}^n N_A = \frac{3n_i}{2}$$

As trivalent impurity is added therefore it will definitely be p-type SC with

$$\text{hole conc}^n p = N_A + \Delta p$$

$$\& e^- \text{ conc}^n n = \Delta n = \Delta p$$

According to Mass action law:

$$n \cdot p = n_i^2$$

$$\Delta n (N_A + \Delta p) = n_i^2$$

$$\Delta p (N_A + \Delta p) = n_i^2$$

$$\Delta p^2 + N_A \Delta p - n_i^2 = 0$$

$$\Delta p^2 + \frac{3}{2} n_i \Delta p - n_i^2 = 0$$

$$(\Delta p + 2n_i) (\Delta p - \frac{n_i}{2}) = 0$$

$$\Delta p = \frac{n_i}{2}, -2n_i$$

But -Ve value is not possible so

$$\Delta p = n_i/2$$

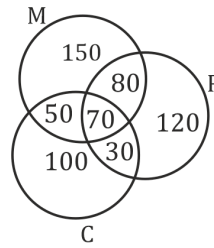
$$p = N_A + \Delta p = 2n_i$$

$$n = \Delta n = \Delta p = \frac{n_i}{2}$$

Hence (c) is correct option

#### Q18 Text Solution:

Total students = 800



No. of students like at least one subject

= No. of students like one subjects + No. of students like two subjects + No. of students like all three subjects

$$= (150 + 120 + 100) + (50 + 30 + 80) + (70) = 600$$

No. of students who like none of the subjects = 800 - 600 = 200

#### Q19 Text Solution:

$$x(t) = m(t) + \cos(2\pi f_0 t)$$

$$\text{So } y_1(t) = x^2(t) = m^2(t) + \cos^2(2\pi f_0 t) + 2m(t) \cos(2\pi f_0 t)$$

- Since  $m(t)$  is a low pass signal  $m^2(t)$  will also be low pass signal.
- $\cos^2(2\pi f_0 t)$  Sinusoid of frequency  $2f_0$
- $2m(t) \cos(2\pi f_0 t)$  DSBSC at  $f_0$  frequency

Now  $y_2(t)$  i.e. output of BPF [centre frequency  $f_0$ ] when  $y_1(t)$  is

$$\text{Input } y_2(t) = 2m(t) \cos(2\pi f_0 t)$$

$$\text{So } y_3(t) = y_2(t) \cdot \cos(2\pi f_0 t)$$

$$\begin{aligned} & 2m(t) \cos^2(2\pi f_0 t) \\ \Rightarrow & 2m(t) \frac{(1 + \cos(4\pi f_0 t))}{2} \\ & m(t) + m(t) \cos(4\pi f_0 t) \end{aligned}$$

So from  $y_3(t)$  the LPF produce  $m(t)$  as output

Since output =  $m(t)$  so bandwidth of output = W

#### Q20 Text Solution:

$$\epsilon_r = 2.25, \quad Z_0 = 300 \Omega, \quad \gamma = 0.6 \text{ mm}$$

$$Z_0 = 120 \sqrt{\frac{\mu_r}{\epsilon_r}} \ln\left(\frac{d}{\gamma}\right)$$

$$\Rightarrow 300 = 120 \sqrt{\frac{1}{2.25}} \ln\left(\frac{d}{\gamma}\right)$$

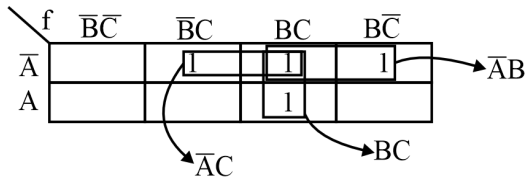
$$\Rightarrow \ln\left(\frac{d}{\gamma}\right) = 3.75 \quad \Rightarrow d = \gamma e^{3.75}$$

$$\Rightarrow d = (e^{3.75} \times 0.6) \text{ mm} = 25.5126 \text{ mm}$$



**Q21 Text Solution:**

Given function is  $f(A, B, C) = \overline{A}B + \overline{A}C + BC$ . KMap of f will be



So in final simplification we get three pairs and result will be  $f(A, B, C) = \overline{A}B + \overline{A}C + BC$

**Q22 Text Solution:**

From the given root locus diagram, the OLTF can be written as,  $G(s)H(s) = \frac{k}{s(s+3-j)(s+3+j)}$

( k = dc gain, s = 0 and -3 ± j are poles).

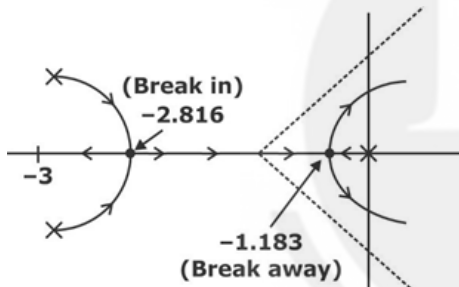
Characteristic equation is,  $1 + G(s)H(s) = 0$

$$k + s(s^2 + 6s + 10) = 0$$

For break point,  $\frac{dk}{ds} = 0 \Rightarrow \frac{dk}{ds} = 3s^2 + 12s + 10 = 0$

$$s = -1.183, -2.816$$

The root locus is as shown



$$\frac{\text{Break in point}}{\text{Break away point}} = \frac{2.816}{1.183} = 2.38$$

**Q23 Text Solution:**

X(t) and Y(t) are orthogonal so  $\overline{X(t)Y(t)} = 0$

So  $u(t) = X(t) + Y(t)$

Now,

$$R_U(\tau) = \overline{u(t)u(t-\tau)}$$

$$= \overline{(X(t)+Y(t))(X(t-\tau)+Y(t-\tau))}$$

$$= \overline{X(t)X(t-\tau) + Y(t)Y(t-\tau)}$$

$$R_U(\tau) = R_X(\tau) + R_Y(\tau)$$

So,  $v(t) = 2X(t) + 3Y(t)$

Now,

$$R_V(\tau) = \overline{v(t)v(t-\tau)}$$

$$= \overline{(2X(t)+3Y(t))(2X(t-\tau)+3Y(t-\tau))}$$

$$= \overline{4X(t)X(t-\tau) + 9Y(t)Y(t-\tau)}$$

$$R_U(\tau) = 4R_X(\tau) + 9R_Y(\tau)$$

$$R_{UV}(\tau) = \overline{u(t).v(t-\tau)}$$

$$= \overline{(X(t)+Y(t))(2X(t-\tau)+3Y(t-\tau))}$$

$$R_{UV}(\tau) = 2R_X(\tau) + 3R_Y(\tau)$$

**Q24 Text Solution:**

$$F = \overline{x}y + x\overline{y}z + xy\overline{z}$$

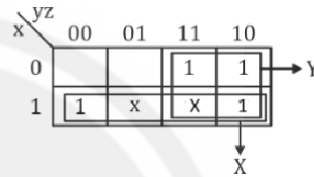
$$= \overline{x}y(z + \overline{z}) + x\overline{y}z + xy\overline{z}$$

$$= \overline{x}yz + \overline{x}y\overline{z} + x\overline{y}z + xy\overline{z}$$

As given x = z = 1, then it will show don't care about the truth table: -

| x | y | z | F |
|---|---|---|---|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | × |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | × |

K-map:-



$$F = x + y$$

**Q25 Text Solution:**

If message is m(t) then DSBSC is  $m(t) \cos \omega_c t$

When message is  $m_1(t)$  then

$$\text{DSBSC} \Rightarrow y_1(t) = m_1(t) \cos \omega_c t$$

When message is  $m_2(t)$  then

$$\text{DSBSC} \Rightarrow y_2(t) = m_2(t) \cos \omega_c t$$

FM signal will be

$$A_c \cos(\omega_c t + 2\pi K_F \int m(\tau) d\tau)$$

FM signal for  $m_1(t)$  message

$$y_1(t) = A_c \cos(\omega_c t + 2\pi K_F \int m_1(\tau) d\tau)$$

FM signal for  $m_2(t)$  message

$$y_2(t) = A_c \cos(\omega_c t + 2\pi K_F \int m_2(\tau) d\tau)$$

New message is  $m_1(t) + m_2(t)$  the DSBSC signal

will be

$$= [m_1(t) + m_2(t)] \cos \omega_c t$$

$$= y_1(t) + y_2(t)$$

If message is  $m_1(t) + m_2(t)$  then

$$\text{FM signal} \Rightarrow$$

$$A_c \cos(\omega_c t + 2\pi K_F \int m_1(\tau) + m_2(\tau) d\tau)$$

$$\neq y_1(t) + y_2(t)$$



**Q26 Text Solution:**

$\epsilon_r = 1, \mu_r = 1$  (Air filled)

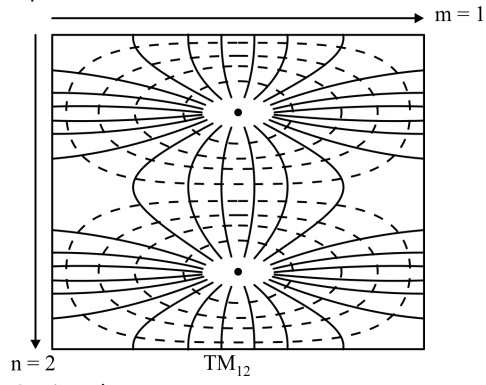
$f = 10 \text{ GHz}, TE_{10} = \text{Dominant mode}$

$$f = 1.25 f_{c_{10}} = 1.25 \frac{c_0}{2a}$$

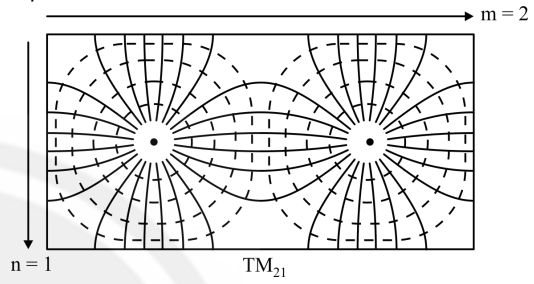
$$a = \frac{1.25 \times 3 \times 10^8}{2 \times 10^{10}} m = 1.875 \text{ cm}$$

**Q27 Text Solution:**

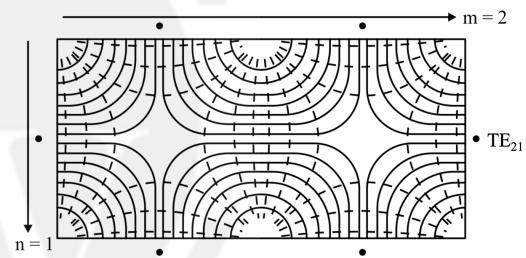
Option (a)



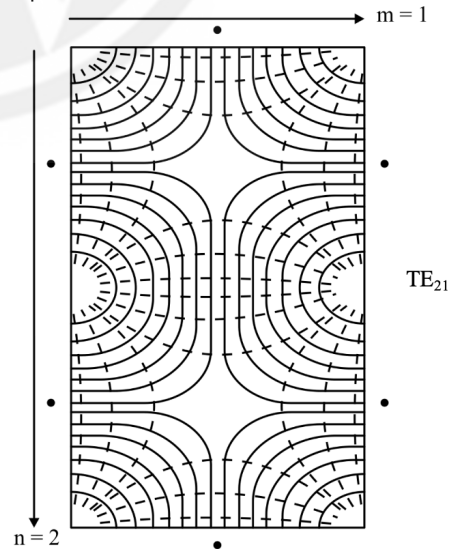
Option (b)



Option (c)



Option (d)



**Q28 Text Solution:**

$$L = \lim_{x \rightarrow 0} \left(\frac{1}{x}\right)^{\tan x}$$

Take log both side

$$\ln L = \lim_{x \rightarrow 0} \tan x \left(-\ln x\right) = \lim_{x \rightarrow 0} \frac{-\ln x}{\cot x}, \left(\frac{\infty}{\infty}\right) \text{ form}$$

using L'hospital rule

$$\lim_{x \rightarrow 0} \frac{-\frac{1}{x}}{-\cos^2 x} = \lim_{x \rightarrow 0} \left(\frac{\sin^2 x}{x}\right) = \lim_{x \rightarrow 0} \left(\frac{\sin x}{x} \cdot \sin x\right) = 0$$

$$\ln L = 0$$

$$L = e^0 = 1$$

**Q29 Text Solution:**

Using the formula:

$$I_{(\max)} = I_{Z(\max)} + I_{L(\min)}$$

$$I_{(\min)} = I_{Z(\min)} + I_{L(\max)}$$

For the Zener diode to operate in worst case condition,

$$I_{(\max)} = \frac{18-8}{100} = \frac{10}{100} = 100 \text{ mA} = I_{Z(\max)}$$

$$P_{Z(\max)} = V_Z I_{Z(\max)} = 100 \times 8 = 800 \text{ mW}$$

Hence, option b,d is correct.

**Q30 Text Solution:**

A demultiplexer selects one of many outputs, whereas a decoder selects an output corresponding to the coded input hence a demultiplexer can be used as a decoder.

Duality can be obtained of any expression by just interchanging the operator  $[\bullet, +]$ .

If any identity (0 or 1) is present in the expression, then interchange 0 by 1 and 1 by 0.

The input to output pin ratio of a multiplexer with  $n$  control inputs is  $2^n : 1$ .

**Q31 Text Solution:**

$$\text{Let } X(z) = \log(1 - 5z)$$

$$\frac{dX(z)}{dz} = \frac{-5}{1-5z}$$

$$\frac{-z dx(z)}{dz} = \frac{5z}{1-5z} = \frac{-5z}{5z-1} = \frac{-1}{1-\frac{1}{5}z^{-1}}$$

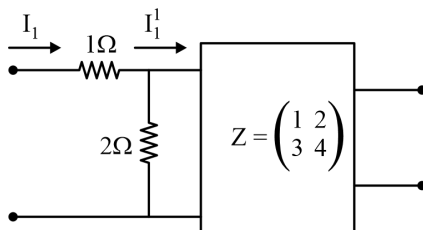
Applying the Inverse Z-transform,

$$nX(n) = \left(\frac{1}{5}\right)^n u(-n-1) \quad \text{since } |z| < \frac{1}{5}$$

$$\text{So, } X(n) = \frac{\left(\frac{1}{5}\right)^n u(-n-1)}{n}$$

$$\text{So, } \alpha = \frac{1}{5}; \beta = +1$$

$$\text{So, } \alpha\beta = \frac{1}{5} = 0.2$$

**Q32 Text Solution:**

$$Z_{12} = \left.\frac{V_1}{I_2}\right|_{I_1=0}$$

$$V_1 = V_1^1 = -2I_1^1 = 1 \times I_1^1 + 2I_2$$

$$-3I_1^1 = 2I_2$$

$$I_1^1 = \frac{-2}{3} I_2$$

$$V_1 = Z_{11} I_1 + Z_{12} I_2$$

$$V_2 = Z_{21} I_1 + Z_{22} I_2$$

$$\begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$Z_{12} = \left.\frac{V_1}{I_2}\right|_{I_1=0} = (-2) \times \frac{-2}{3} = \frac{4}{3}$$

$$Z_{12} = \frac{4}{3} = 1.33 \Omega$$

**Q33 Text Solution:**

At no applied bias, diode remains at equilibrium with net current  $I = 0$ .

At equilibrium diffusion current flows from p to n direction & drift current flows from n to p direction where  $I_{\text{drift}} = I_0$

$$I_{\text{diff}} + I_{\text{drift}} = 0$$

$I_{\text{diff}} = -I_{\text{drift}} = -I_0$  (-Ve sign signifies that current is from p to n (where  $I_{\text{drift}}$  is from n to p).

$$I_{\text{diff}} = 10^{-8} \text{ A from p to n}$$

$$I_{\text{diff}} = 10 \text{ nA from p to n}$$

**Q34 Text Solution:**

We know that,

$$\text{sgn}(t) \Leftrightarrow \frac{2}{j\omega}$$

By using the duality property:

$$\frac{2}{jt} \Leftrightarrow 2\pi \times \text{sgn}(-\omega)$$

$$\frac{1}{\pi t} \Leftrightarrow j \text{sgn}(-\omega)$$

$\text{sgn}(\omega)$  is an odd function, then  $\text{sgn}(-\omega) = -\text{sgn}(\omega)$

$$\therefore \frac{1}{\pi t} \Leftrightarrow -j \text{sgn}(\omega)$$

$$\therefore h(t) = \frac{1}{\pi t} \Leftrightarrow -j \text{sgn}(\omega) = H(\omega)$$

$$h(t) = \frac{1}{\pi t}$$

**Q35 Text Solution:**

$$1. \text{Var}(aX) = a^2 (\text{Var}(X))$$

2. for independent X and Y

$$\text{Var}(aX \pm bY) = a^2 \text{Var}(X) + b^2 \text{Var}(Y)$$

$$(A) \text{Var}(2X) = 2^2 \times \text{Var}(X) = 4 \times 4 = 16$$

(B)

$$\text{Var}(X - Y) = \text{Var}(X) + \text{Var}(Y) = 4 + 9 = 13$$

(C)

$$\text{Var}(2X + 3Y) = 2^2 \text{Var}(X) + 3^2 \text{Var}(Y) = 4 \times 4 + 9 \times 9 = 97$$

(D)

$$\text{Var}\left(\frac{Y}{3}\right) = \text{Var}\left(\frac{1}{3}Y\right) = \left(\frac{1}{3}\right)^2 \text{Var}Y = \frac{1}{9} \times 9 = 1$$



**Q36 Text Solution:**

$$S = \frac{1}{2} - \frac{1}{6} + \frac{1}{24} - \frac{1}{120} + \dots$$

$$= \frac{1}{2!} - \frac{1}{3!} + \frac{1}{4!} - \frac{1}{5!} + \dots$$

$$= 1 - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!} + \frac{1}{4!} - \frac{1}{5!} + \dots$$

$$= e^{-x} \Big|_{x=1} = e^{-1} = 0.3678 \approx 0.368$$

**Q37 Text Solution:**

Given:  
 $x + y + 5z = 3$   
 $x + 2y + 2z = 5$   
 $2x + 4y + 4z = k$   
 $A X = B$

$$[A|B] = \begin{bmatrix} 1 & 1 & 5 & 3 \\ 1 & 2 & 2 & 5 \\ 2 & 4 & 4 & k \end{bmatrix}$$

For the system to have infinitely many solutions,

$$\text{Rank}(A) = \text{Rank}(A|B) < 3$$

All  $3 \times 3$  minors of  $[A|B]$  should be zero.

consider a  $3 \times 3$  minor of  $[A|B]$

$$\begin{vmatrix} 1 & 5 & 3 \\ 2 & 2 & 5 \\ 4 & 4 & k \end{vmatrix} = 0$$

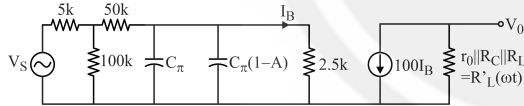
$$1(2k - 20) - 5(2k - 20) + 3(0) = 0$$

$$2k - 20 = 0$$

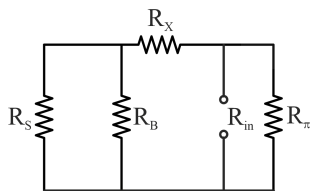
$$k = 10$$

**Q38 Text Solution:**

Using small signal analysis



where  $R'_L = (100k) || 8k || 5k = 2.98 \text{ k}\Omega$



$$A = \frac{V_0}{V_\pi} = \frac{-\beta I_B R'_L}{I_B r_\pi} = \frac{-100 \times 2.98 \text{ k}\Omega}{2.5 \text{ k}\Omega} = -119.4$$

$$C_{eq} = C_\pi + C_\mu(1 - A) = 7 + 1(1 + 119.4) = 127.4$$

pF

$$R'_m = [(R_S || R_B) + R_X] || R_\pi = 1.64 \text{ k}\Omega$$

$$f_H = \frac{1}{2\pi R'_m C_{eq}} = 762.1 \text{ kHz}$$

**Q39 Text Solution:**

$$x(n) \xleftrightarrow{DTFT} X(e^{j\omega})$$

$$x(e^{j\omega}) = \sum_{n=-\infty}^{\infty} x(n) e^{-j\omega n}$$

$$x(e^{j0}) = \sum_{n=-\infty}^{\infty} x(n)$$

Since  $nX(n) \xleftrightarrow{DTFT} j \frac{dX(e^{j\omega})}{d\omega}$

or  $j \frac{dX(e^{j\omega})}{d\omega} = \sum_{n=-\infty}^{\infty} nX(n) e^{-j\omega n}$

or  $j \frac{dX(e^{j\omega})}{d\omega} \Big|_{\omega=0} = \sum_{n=-\infty}^{\infty} nX(n)$

So,  $A = \frac{j \frac{dX(e^{j\omega})}{d\omega} \Big|_{\omega=0}}{X(e^{j0})}$

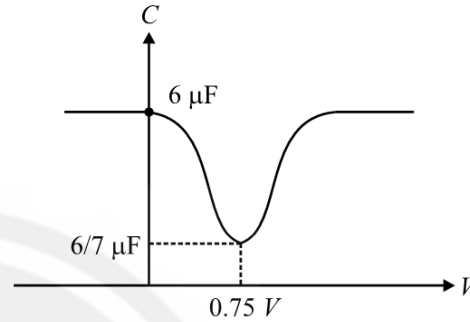
From graph given,  $\frac{dX(e^{j\omega})}{d\omega} \Big|_{\omega=0} = 0$  and  $X(e^{j0}) = 1$

= 1

So,  $A = \frac{0}{1} = 0$

**Q40 Text Solution:**

Lets draw the C-V characteristic:



From characteristic

$$C_{Max} = 6 \mu F = C_{ox}$$

$$C_{Min} = \frac{6}{7} \mu F$$

=  $C_{ox}$  in series with  $(C_{dep})_{min}$

$$(C_{dep})_{min} = 1 \mu F$$

$$\frac{\epsilon A}{W_{Max}} = 1 \mu F = 10^{-6} F$$

$$\frac{\epsilon}{W_{Max}} = \frac{10^{-6} F}{A} = \frac{10^{-6} F}{1 \text{ cm}^2} = 10^{-6} F/\text{cm}^2$$

$E_{Max}$  at surface =

$$\frac{q}{\epsilon} N_S \cdot W_{Max}$$

$$= \frac{q}{\left(\frac{\epsilon}{W_{Max}}\right)} \cdot N_S = \frac{1.6 \times 10^{-19}}{10^{-6}} \times 2 \times 10^{16}$$

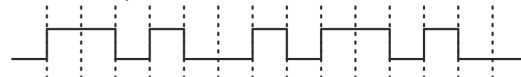
$$E_{Max} = 3.2 \times 10^3 \text{ V/cm} = 3.2 \text{ KV/cm}$$

**Q41 Text Solution:**

For An EX-NOR gate output is high when

Both inputs are same i.e. both 0 and both 1,

Hence output waveform is



The output Y is repeating itself after  $8\mu\text{sec}$

Hence,  $T_0 = 8 \mu\text{sec}$

$$f = \frac{1}{T_0} = \frac{1}{8\mu} = 125 \text{ kHz}$$



**Q42 Text Solution:**

To calculate average power of  $V_2$  we have to find PSD of O/P

$$PSD_{O/P} = PSD_{I/P} \cdot |H(\omega)|^2$$

We can see that  $H(\omega) = \frac{R}{R+j\omega L}$

So,

$$PSD_0 = \frac{N_0}{2} \cdot \left( \frac{R^2}{R^2+4\pi^2 f^2 L^2} \right)$$

$$P_{avg} = \int_{-\infty}^{\infty} PSD_0 df$$

$$= \frac{N_0}{2} R^2 \int_{-\infty}^{\infty} \frac{1}{R^2+4\pi^2 f^2 L^2} df$$

$$= \frac{N_0}{2} \frac{R^2}{4\pi^2 L^2} \int_{-\infty}^{\infty} \frac{1}{\frac{R^2}{4\pi^2 L^2} + f^2}$$

$$= \frac{N_0}{2} \frac{R^2}{4\pi^2 L^2} \frac{1}{R/2\pi L} \left[ \tan^{-1} \frac{f}{R/2\pi L} \right]_{-\infty}^{\infty}$$

$$\Rightarrow \frac{N_0}{2} \cdot \frac{R}{2\pi L} (\pi)$$

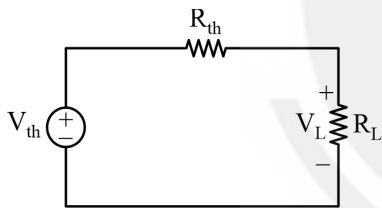
$$\Rightarrow \frac{N_0 R}{4L}$$

**Q43 Text Solution:**

For maximum power transfer,

$$R_L = R_{th} = 10\Omega$$

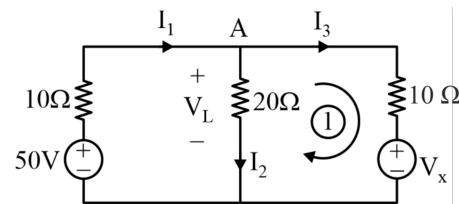
$$V_{th} = 50V$$



$$V_L = \frac{V_{th} \times R_L}{R_L + R_{th}}$$

$$V_L = \frac{50 \times 10}{10 + 10} = 25V$$

Now in circuit,



Voltage across 20Ω resistor =  $V_L = 25V$

$$I_1 = \frac{50 - V_L}{10} = \frac{50 - 25}{10} = 2.5 A$$

$$I_2 = \frac{V_L}{20} = \frac{25}{20} = 1.25 A$$

KCL at node A,

$$I_3 = I_1 - I_2 = 2.5 - 1.25 = 1.25 A$$

KVL in loop (1)

$$-V_L + 10I_3 + V_x = 0$$

$$-25 + 10(1.25) + V_x = 0$$

$$V_x = 12.5 V$$

**Q44 Text Solution:**

$$\text{Let } \frac{Y(s)}{U(s)} = \frac{10(s+3)}{(s^3+6s^2+11s+6)} \cdot \frac{X(s)}{X(s)}$$

$$\text{Then, } Y(s) = (s + 3) X(s) \quad \dots(i)$$

$$10U(s) = (s^3 + 6s^2 + 11s + 6) X(s)$$

...(ii)

From inverse Laplace transform,

$$\frac{d^3 x(t)}{dt^3} + 6 \frac{d^2 x(t)}{dt^2} + 11 \frac{dx(t)}{dt} + 6x(t) = 10u(t)$$

...(iii)

$$\text{Let } \dot{x} = x_1 \Rightarrow \dot{x}_1 = x_2 \Rightarrow \dot{x}_2 = x_3$$

So, from equation (iii),

$$x_3 + 6x_2 + 11x_1 + 6x_1 = 10u(t) \quad \dots(iv)$$

$$= -6x_1(t) - 11x_2(t) - 6x_3(t) + 10u(t)$$

$$\dot{x}_2 = x_1$$

$$\dot{x}_1 = x_1$$

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix}, B = \begin{bmatrix} 0 \\ 0 \\ 10 \end{bmatrix} = \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix}$$

Also,  $Y(s) = (s + 3) X(s)$

$$y(t) = +3x_1 = x_2 + 3x_1$$

$$y(t) = 3x_1(t) + x_2(t) + 0 \cdot x_3(t)$$

$$C = [3 \ 1 \ 0] = [C_1 \ C_2 \ C_3]$$

$$\frac{b_1 + C_1}{b_2 + C_2} = \frac{0+3}{0+1} = 3.0$$

**Q45 Text Solution:**

Given,  $x_1(t) = te^{-|t|}$

$$e^{-|t|} = e^{-t} u(t) + e^t u(-t)$$

$$e^{-|t|} \xleftrightarrow{FT} \frac{1}{1+j\omega} + \frac{1}{1-j\omega} = \frac{2}{1+\omega^2}$$

$$t x(t) \xleftrightarrow{FT} j \frac{d}{d\omega} X(\omega)$$

$$j \frac{d}{d\omega} \left( \frac{2}{1+\omega^2} \right) = \frac{-4j\omega}{(1+\omega^2)^2}$$

$$X_1(\omega) = \frac{-4j\omega}{(1+\omega^2)^2} \quad \dots(i)$$

$$\text{Also, } x_2(t) = \frac{t}{(1+t^2)^2}$$

$$e^{-|t|} \xleftrightarrow{FT} \frac{2}{1+\omega^2}$$

$$te^{-|t|} \xleftrightarrow{FT} \frac{-j4\omega}{(1+\omega^2)^2}$$

By the duality property,

$$x(t) \xleftrightarrow{FT} X(\omega)$$

$$x(t) \xleftrightarrow{FT} 2\pi X(-\omega)$$

$$\frac{-4jt}{(1+t^2)^2} \xleftrightarrow{FT} 2\pi(-\omega) e^{-|\omega|}$$

$$\text{Or } x_2(t) = \frac{t}{(1+t^2)^2} \xleftrightarrow{FT} \frac{2\pi}{4j} \times \omega \times e^{-|\omega|}$$

$$X_2(\omega) = -\frac{\pi}{2} j\omega e^{-|\omega|}$$

$$\frac{X_1(\omega)}{X_2(\omega)} = \frac{-4j\omega}{(1+\omega^2)^2} \times \frac{1}{\frac{-\pi}{2} j\omega e^{-|\omega|}} = \frac{8}{\pi} \frac{1}{(1+\omega^2)^2} \times \frac{1}{e^{-|\omega|}}$$

At  $\omega = \pi$



$$\frac{8}{\pi} \times \frac{1}{(1+\pi^2)^2} \times \frac{1}{e^{-\pi}} = 0.4987 \approx 0.50$$

**Q46 Text Solution:**

Given:

$$L^{-1} \left\{ \frac{s+3}{s^2-4s+13} \right\} = e^{2t} \cdot \cos 3t + \alpha \cdot e^{2t} \cdot \sin 3t$$

$$\Rightarrow \frac{s+3}{s^2-4s+13} = L \{ e^{2t} \cdot \cos 3t \} + \alpha \cdot L \{ e^{2t} \cdot \sin 3t \}$$

$$\therefore L \{ \sin at \} = \frac{a}{s^2+a^2}$$

$$\Rightarrow L \{ e^{bt} \cdot \sin at \} = \frac{a}{(s-b)^2+a^2}$$

Similarly

$$L \{ e^{bt} \cdot \cos at \} = \frac{s-b}{(s-b)^2+a^2}$$

$$\therefore \frac{s+3}{(s-2)^2+9} = \frac{s-2}{(s-2)^2+9} + \frac{\alpha \cdot (3)}{(s-2)^2+9}$$

$$\Rightarrow \frac{s+3}{(s-2)^2+9} = \frac{s+(3\alpha-2)}{(s-2)^2+9}$$

$$\Rightarrow 3 = 3\alpha - 2$$

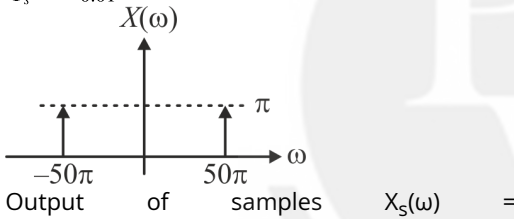
$$\Rightarrow \alpha = \frac{5}{3} = 1.667$$

$$\therefore \alpha = 1.667$$

**Q47 Text Solution:**

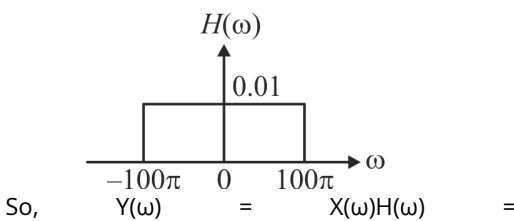
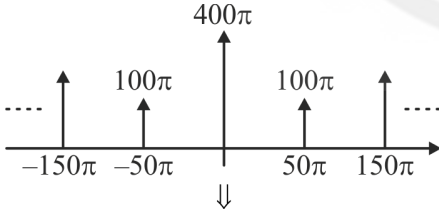
Sampling frequency ( $\omega_s$ ) =

$$\frac{2\pi}{T_s} = \frac{2\pi}{0.01} = 200\pi \text{ rad/sec}$$



$$\frac{1}{T_s} \sum_{n=-\infty}^{\infty} X(\omega - 100\pi)$$

$$= 100 \sum_{n=-\infty}^{\infty} X(\omega - 200\pi n)$$



$$Y(\omega) = X(\omega)H(\omega) = 4\pi \delta(\omega) + \pi[\delta(\omega + 50\pi) + \delta(\omega - 50\pi)]$$

Gives  $y(t)$  after using inverse Fourier transform,

$$y(t) = 2 + \cos(500t)$$

Therefore,  $A = 2$

**Q48 Text Solution:**

We know that 20 dB/decade = 6 dB/octave  
So, '2' poles at origin 1 zero at  $\omega_1 = 2$  rad/sec, 1 pole at  $\omega_2 = 20$  rad/sec

(Initial slope = -40 dB/dec)

$$T(s) = \frac{k(1+\frac{s}{2})}{s^2(1+\frac{s}{20})}$$

At  $\omega_1 = 2$ , magnitude = 0 dB

from approximate Bode analysis,  
Gain at ( $\omega_0$ ) = 0 dB = 20 log(k) + slope  $\times$  log( $\omega_0$ )

$$(\omega_0 = 2 \text{ rad/sec})$$

$$0 = 20 \log k - 40 \log 2$$

$$k = 4$$

So,  $T(s) = \frac{4(1+\frac{s}{2})}{s^2(1+\frac{s}{20})} = G(s)$  for an input

$$\frac{5t^2}{2} u(t)$$

$e_{ss}$  for  $\frac{\lambda t^2}{2} u(t) = \frac{\lambda}{k_a}$  where,  $k_a =$

$$\lim_{s \rightarrow 0} s^2 G(s)$$

$$k_a = \lim_{s \rightarrow 0} s^2 \times \frac{4}{s^2} \frac{(1+\frac{s}{2})}{(1+\frac{s}{20})} = 4$$

So, for  $\frac{5t^2}{2} u(t)$   $e_{ss} = \frac{5 \times 1}{k_a} = \frac{5}{4} = 1.25$

**Q49 Text Solution:**

$$\frac{V_0}{V_{in}} = \frac{(-R_2 \parallel \frac{1}{sC})}{R_1} = \frac{-R_2/R_1}{1+sR_2C} = \frac{-R_2/R_1}{1+j\omega CR_2}$$

If  $\omega \gg \frac{1}{R_2C}$ ;

$$\frac{V_0}{V_{in}} = \frac{-R_2/R_1}{1+j\omega CR_2} = \frac{-R_2/R_1}{1+j\omega(1/R_2C)}$$

For  $\omega \gg \frac{1}{R_2C}$ ;  $[\omega(1/R_2C)] \gg \gg 1$ , so gain can be approximated to

$$\frac{V_0}{V_{in}} = \frac{(-R_2/R_1)}{j\omega R_2C} = \frac{-1}{j\omega R_1C}$$

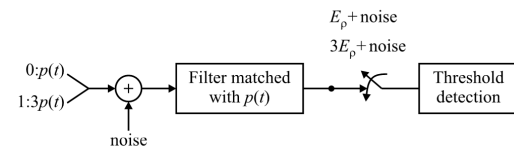
Or  $V_0 = \frac{-1}{R_1C} \int V_{in} dt$  acts as integrator.

If  $\omega \ll \frac{1}{R_2C}$ ;

$$\frac{V_0}{V_{in}} = \frac{(-R_2/R_1)}{1}$$

Or  $|\frac{V_0}{V_{in}}| = \frac{R_2}{R_1} \Rightarrow V_0 = (\frac{R_2}{R_1}) V_{in}$  acts as amplifier.

**Q50 Text Solution:**

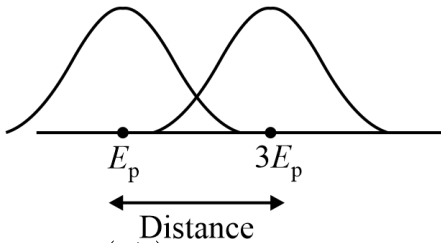


Noise at input of match filter has Variance  $\frac{N_0}{2}$   
Noise at output of match filter has Variance  $\frac{N_0}{2} E_\rho$

At input of threshold device  $E_\rho + \text{noise}$  (gaussian noise at  $E_\rho$ )

$3 E_\rho + \text{noise}$  (gaussian noise at  $3 E_\rho$ )





$$P_e = Q\left(\frac{d/2}{\sigma}\right)$$

$$= Q\left(\frac{2E_p/2}{\sqrt{\frac{N_0}{2}} \epsilon_p}\right)$$

$$= Q\left(\sqrt{\frac{2E_p}{N_0}}\right)$$

Now bit 0  $p(t)$  energy  $E_p$

bit 1  $3p(t)$  energy  $9E_p$

So average bit energy

$$E_b = \frac{E_p + 9E_p}{2}$$

$$E_b \Rightarrow 5E_p$$

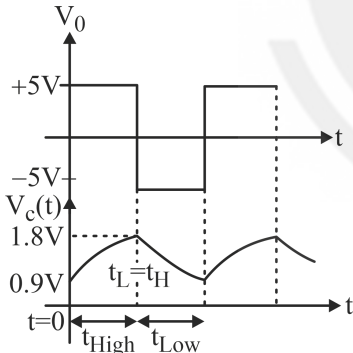
$$\text{So } P_e = Q\left(\sqrt{\frac{2E_{b/s}}{N_0}}\right)$$

#### Q51 Text Solution:

Given,  $V_{LT} = 0.9V$ ,  $V_{UT} = 1.8V$

$C = 0.4 \mu F$ ,  $R = 10k$ ,  $\pm V_{sat} = \pm 5V$

The circuit is behaving as a astable multivibrator,



To find  $t_{High}$ ,

Assume  $t = 0$  and  $t = t_H$  as shown,

$$V_c(0^+) = 0.9V, V_c(\infty) = +5V$$

$$V_c(t_{High}) = 1.8V$$

$$V_c(t) = V_c(\infty) + [V_c(0^+) - V_c(\infty)] e^{-t/RC}$$

$$RC = 10^4 \times 0.4 \times 10^{-6} = 0.4 \times 10^{-2} \text{ sec.}$$

$$V_c(t_{High}) = 5 + (0.9 - 5) e^{-t/RC}$$

$$1.8 = 5 - 4.1 e^{-t/RC}$$

$$e^{-t_H/RC} = 0.7805 \quad -t_H/RC = \ln(0.7805) =$$

$$-0.2478$$

$$t_H = 0.2478 \times 4 \text{ msec}$$

$$t_H = 0.9913 \text{ msec}$$

#### Q52 Text Solution:

So we know that  $P_e = Q\left(\frac{d/2}{\sigma}\right)$

$d$  Distance b/w the symbols in constellation diagram

$\sigma$  Standard deviation of noise

$d$  From diagram  $S_1(1, 1)$  and  $S_0(-1, -1)$

$$d = \sqrt{2^2 + 2^2} \Rightarrow \sqrt{8}$$

Variance of noise  $(\sigma^2) = \frac{1}{2}$

$$\text{So } \sigma = 1/\sqrt{2}$$

$$\text{So } P_e = Q\left(\frac{\sqrt{8}}{2} / 1/\sqrt{2}\right)$$

$$Q(2)$$

#### Q53 Text Solution:

Given: DE is  $(D^2 + 1)y = \sin t$

A.E:  $D^2 + 1 = 0$

$$D = \pm i$$

$$\Rightarrow y_c = c_1 \cos t + c_2 \sin t$$

$$\text{PI: } (y_p) = \frac{1}{D^2 + 1} \sin(t) \quad D^2 - 1^2$$

$$= \frac{1}{-1+1} \sin(t) \quad (\text{Denominator} = 0)$$

$$= \frac{t}{2D} \sin t = \frac{t}{2} (-\cos t) = -\frac{t}{2} \cos t$$

$$y = y_c + y_p$$

$$y = c_1 \cos t + c_2 \sin t - \frac{t}{2} \cos t$$

$$y(0) = c_1 \times 1 + 0 - 0$$

$$\Rightarrow \boxed{0 = c_1}$$

$$y' = -c_1 \sin t + c_2 \cos t - \frac{1}{2} \cos t - \frac{t}{2} (-\sin t)$$

$$y'(0) = -0 + c_2 - \frac{1}{2}$$

$$0 = c_2 - \frac{1}{2}$$

$$\Rightarrow \boxed{c_2 = \frac{1}{2}}$$

$$y = \frac{1}{2} \sin t - \frac{t}{2} \cos t$$

$$y(\pi) = \frac{1}{2} \sin \pi - \frac{\pi}{2} \cos \pi = \frac{\pi}{2} = 1.57$$

#### Q54 Text Solution:

$$Q_{n+1} = D = \overline{X} Q_n + Y \overline{Q_n} \quad (Z = Q_n)$$

Comparing with characteristic equation of JK-FF,

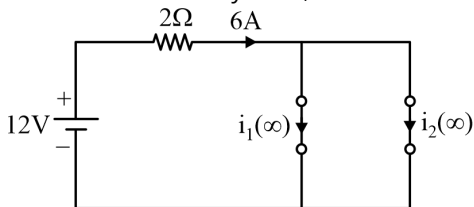
$$Q_{n+1} = J \overline{Q_n} + \overline{K} Q_n$$

$$X = K, Y = J$$



**Q55 Text Solution:**

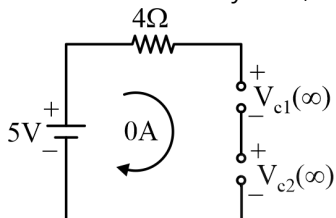
For circuit 1 at steady state,



$$I(\infty) = i_1(\infty) + i_2(\infty) = \frac{12}{2} = 6A$$

$$\text{From current divisions } i_1(\infty) = 6 \times \frac{2}{2+1} = \frac{12}{3} = 4A$$

For circuit 2 at steady state,



From voltage division

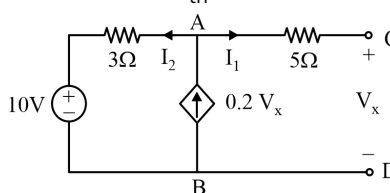
$$\text{Rule, } V_{c2}(\infty) = 5 \times \frac{3}{3+6}$$

$$V_{c2}(\infty) = \frac{15}{9} = \frac{5}{3}V$$

$$\frac{V_{c2}(\infty)}{i_1(\infty)} = \frac{5}{3} \times \frac{1}{4} = \frac{5}{12} \Omega = 416.67 \text{ m}\Omega$$

**Q56 Text Solution:**

Calculation for  $V_{th}$



$$V_{th} = V_x$$

$$I_1 = 0 \text{ [open circuit]}$$

$$I_2 = 0.2 V_x$$

$$V_{AB} = V_x = V_{th}$$

Apply KVL in left loop,

$$-V_x + 3I_2 + 10 = 0 \quad \dots(1)$$

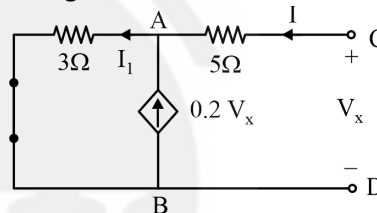
Put  $I_2$  in equation (1)

$$-V_x + 3(0.2V_x) + 10 = 0$$

$$V_x = 25V \quad V_{th} = 25V$$

Calculation for  $R_{th}$

Voltage source short circuit



KCL at Node A,

$$I_1 = 0.2V_x + I$$

Apply KVL in total loop,

$$-V_x + 5I + 3(I_1) = 0$$

$$-V_x + 5I + 3(0.2V_x + I) = 0 \quad [ I_1 = 0.2V_x + I ]$$

$$-V_x + 5I + 0.6V_x + 3I = 0$$

$$-0.4V_x + 8I = 0$$

$$0.4V_x = 8I$$

$$R_{th} = \frac{V_x}{I} = \frac{8}{0.4} = 20\Omega$$

**Q57 Text Solution:**

$$\frac{Y(s)}{R(s)} = \frac{2}{(s^3 + 5s^2 + 6s + 3)} \left( \frac{K_p s + K_i}{s} \right)$$

$$= \frac{2(K_p s + K_i)}{s^4 + 5s^3 + 6s^2 + 3s}$$

$$\frac{Y(s)}{R(s)} = \frac{2K_p s + 2K_i}{s^4 + 5s^3 + 6s^2 + (3 + 2K_p)s + 2K_i}$$

Characteristic Equation:

$$s^4 + 5s^3 + 6s^2 + (3 + 2K_p)s + 2K_i = 0$$



$$\begin{array}{r|l}
 s^4 & 1 & 6 \\
 s^3 & 5 & (3 + 2K_P) \\
 s^2 & \frac{(30-3-2K_P)}{5} & 2K_i \\
 s^1 & \frac{\left(\frac{27-2K_P}{5}\right)(3+2K_P)-10K_i}{\left(\frac{27-2K_P}{5}\right)} & 0 \\
 s^0 & 2K_i & 0
 \end{array}$$

$$2K_i > 0 \quad K_i > 0 \quad \dots(1)$$

$$27 - 2K_P > 0 \quad K_P < 13.5 \quad \dots(2)$$

$$\frac{\left(\frac{27-2K_P}{5}\right)(3+2K_P)-10K_i}{\left(\frac{27-2K_P}{5}\right)} = (3 + 2K_P) - \frac{50K_i}{27-2K_i} > 0$$

$$(3 + 2K_P) > \frac{50K_i}{27-2K_i}$$

$$81 - 6K_P + 54K_P - 4K_P^2 > 50K_i$$

$$-4K_P^2 + 48K_P + 81 > 50K_i$$

$$K_i < \frac{-4K_P^2 + 48K_P + 81}{50}$$

$$\frac{dK_i}{dK_P} = -8K_P + 48 = 0$$

$$K_P = 6$$

Therefore,  $K_i = 4.5$

Hence, option A and B both are correct.

**Q58 Text Solution:**

$$x^3 - 5x + 3 = 0$$

As sum of the root is  $\left(\frac{-b}{a}\right)$

$$\text{So, } a + b + c = \frac{0}{1} = 0$$

$$\therefore \begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix}$$

$$c_1 \rightarrow c_1 + c_2 + c_3$$

$$\Rightarrow \begin{vmatrix} a+b+c & b & c \\ a+b+c & c & a \\ a+b+c & a & b \end{vmatrix}$$

$$\Rightarrow \begin{pmatrix} a+b+c \\ a+b+c \\ a+b+c \end{pmatrix} \begin{vmatrix} 1 & b & c \\ 1 & c & a \\ 1 & a & b \end{vmatrix}$$

$$\Rightarrow 0$$

**Q59 Text Solution:**

Due to Early effect:

(i)  $I_E$

(ii)  $I_C$

(iii)  $\alpha, \beta$  &  $\gamma$

Thus (c) is not correct option.

**Q60 Text Solution:**

$$\text{For solenoidal } \vec{\nabla} \cdot \vec{A} = 0$$

$$\text{For Harmonic } \nabla^2 \vec{A} = \vec{0}$$

$$\vec{\nabla} \times (\vec{\nabla} \times \vec{A}) = \vec{\nabla} (\vec{\nabla} \cdot \vec{A}) - \nabla^2 \vec{A}$$

$$\vec{\nabla} \times (\vec{\nabla} \times \vec{A}) = 0$$

**Q61 Text Solution:**

Maximum electric field at surface inside substrate is

$$E_0 = \frac{2\phi_s}{W} = \frac{2 \times 0.45}{10 \mu\text{m}} = \frac{0.9}{10 \times 10^{-4} \text{ cm}} = 900 \text{ V/cm}$$

From continuity equation

$$E_2 \epsilon_{SiO_2} = E_1 \epsilon_{Si} \quad [E_2 \text{ electric field at surface inside } SiO_2]$$

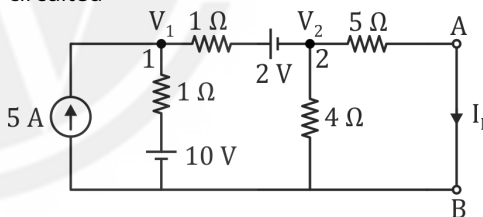
$$E_2 = \frac{\epsilon_{Si}}{\epsilon_{SiO_2}} E_1 = 2.5 \times 900 = 2250 \text{ V/cm}$$

$$= 2.25 \text{ KV/cm}$$

As inside oxide layer, electric field is constant therefore  $E_{\text{max}}$  inside oxide layer will be equal to  $E_2$ .

**Q62 Text Solution:**

For Norton current load, terminal is short circuited



KCL at node 1,

$$5 = \frac{V_1 - 10}{1} + \frac{V_1 - (V_2 + 2)}{1}$$

$$5 = V_1 - 10 + V_1 - V_2 - 2$$

$$2V_1 - V_2 = 17 \quad \dots(1)$$

KCL at node 2,

$$\frac{V_2}{4} + \frac{V_2}{5} + \frac{V_2 + 2 - V_1}{1} = 0$$

$$0.25V_2 + 0.2V_2 + V_2 - V_1 + 2 = 0$$

$$1.45V_2 - V_1 = -2$$

$$2.90V_2 - 2V_1 = -4 \quad \dots(2)$$

Solving (1) and (2),

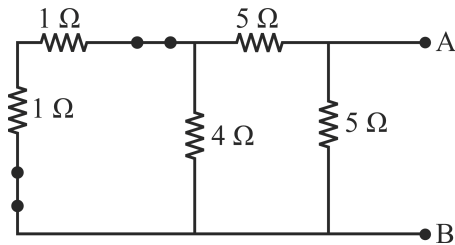
$$1.9V_2 = 13$$

$$V_2 = \frac{13}{1.9} = 6.84 \text{ volts}$$

$$\text{Norton's current } I_N = \frac{V_2}{5} = \frac{6.84}{5} = 1.368 \text{ A}$$

**For  $R_N$**





$$R_N = [(1 + 1) || 4 + 5] || 5$$

$$R_N = 2.79 \Omega$$

**Q63 Text Solution:**

$$Z_0 = 50, Z_L = R_L + jX_L, \text{VSWR} = 2$$

$$|\Gamma_L| = \frac{2-1}{2+1} = \frac{1}{3} \dots (1)$$

$$\Gamma_L = \frac{Z_L - Z_0}{Z_L + Z_0} = \frac{(R_L - 50) + jX_L}{(R_L + 50) + jX_L} \Rightarrow |\Gamma_L| = \sqrt{\frac{(R_L - 50)^2 + X_L^2}{(R_L + 50)^2 + X_L^2}}$$

3....(2)

Equating Equation (1) & (2)

$$\frac{(R_L - 50)^2 + X_L^2}{(R_L + 50)^2 + X_L^2} = \left(\frac{1}{3}\right)^2$$

$$\Rightarrow 9R_L^2 + 9X_L^2 + 9 \times 2500 - 900R_L = R_L^2 + 2500 + 100X_L + X_L^2$$

$$\Rightarrow R_L^2 - 125R_L + 2500 + X_L^2 = 0$$

$$\Rightarrow R_L^2 - 2(62.5)R_L + 3906.25 + X_L^2 + 2500 - 3906.25 = 0$$

$$\Rightarrow (R_L - 62.5)^2 + X_L^2 = 1406.25 = (37.5)^2$$

$$(R_L - 62.5)^2 + X_L^2 = (37.5)^2$$

$$R = 37.5 \Omega$$

**Q64 Text Solution:**

We know that  $CH^T = 0$  for a valid code word

$$(0100011) \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & b & 1 \\ 1 & 0 & a \end{bmatrix} \Rightarrow [0 + 1 + 1, 1 + b + 0, 0 + 1 + a]$$

For  $CH^T = (000)$

So in modulo 2 addition 0 is result when we add two 1's

So,

$$1 + b = 0, b = 1$$

$$1 + a = 0, a = 1$$

**Q65 Text Solution:**

$$d\vec{s} = r^2 \sin \theta d\theta d\phi \hat{a}_r |_{r=2}$$

$$I = \iint \vec{J} \cdot d\vec{s} = \iint r^3 \sin \theta d\theta d\phi |_{r=2} = 8 \int_0^{\pi/2} \sin \theta d\theta \int_{\pi/6}^{\pi/3} d\phi$$

$$= 8(-\cos \theta)_0^{\pi/2} \left(\frac{\pi}{3} - \frac{\pi}{6}\right) = 2(1)\left(\frac{\pi}{6}\right) = \frac{\pi}{3} = 1.05 \text{ A.}$$



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